



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL
SENIOR CERTIFICATE/
NASIONALE
SENIOR SERTIFIKAAT**

GRADE/GRAAD 12

SEPTEMBER 2014

**MATHEMATICS P1/WISKUNDE V1
MEMORANDUM**

MARKS/PUNTE: 150

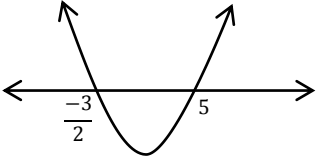
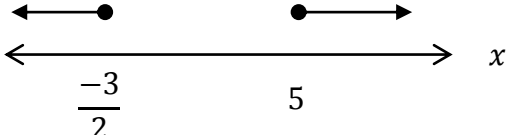
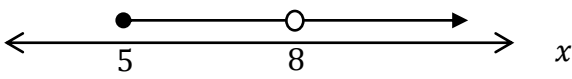
Hierdie memorandum bestaan uit 16 bladsye./
This memorandum consists of 16 pages.

NOTE/LET OP:

- If a candidate answered a question TWICE, mark the FIRST attempt ONLY.
Indien 'n kandidaat 'n vraag TWEE keer beantwoord het, merk SLEGS die EERSTE poging.
- Consistent accuracy applies in ALL aspects of the memorandum.
Volgehoue akkuraatheid geld deurgaans in ALLE aspekte van die memorandum.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out attempt.
Indien 'n kandidaat 'n poging vir 'n vraag deurgetrek het en nie die vraag weer beantwoord het nie, merk die poging wat deurgetrek is.
- The mark for substitution is awarded for substitution into the correct formula.
Die punt vir substitusie word toegeken vir substitusie in die korrekte formule.

QUESTION 1/VRAAG 1

1.1.1	$3x^2 - 7x = 0$ $x(3x - 7) = 0$ $x = 0 \text{ or/of } x = \frac{7}{3}$ <p>OR/OF</p> $3x^2 - 7x = 0$ $x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(3)(0)}}{2(3)}$ $x = 0 \text{ or/of } x = \frac{7}{3}$	<p>Note/Let op: If divided by x/indien deel deur x $\therefore x = \frac{7}{3}$ only/slegs, 0 marks/punte.</p>	<ul style="list-style-type: none"> ✓ factors/faktore ✓ x-values/waardes ✓ substitution/substitusie ✓ x-values/waardes <p style="text-align: right;">(2)</p>
1.1.2	$5x^2 = 3x + 6$ $5x^2 - 3x - 6 = 0$ $x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(5)(-6)}}{2(5)}$ $x = \frac{3 \pm \sqrt{129}}{10}$ $x = -0,84 \text{ or/of } x = 1,44$	<p>Penalise 1 mark for incorrect rounding off. Penaliseer 1 punt vir verkeerde afronding.</p>	<ul style="list-style-type: none"> ✓ standard form/standaardvorm ✓ substitution/substitusie ✓✓ x-values/waardes <p style="text-align: right;">(4)</p>
1.1.3	$3x^{\frac{2}{3}} - 13x^{\frac{1}{3}} - 10 = 0$ $\left(3x^{\frac{1}{3}} + 2\right)\left(x^{\frac{1}{3}} - 5\right) = 0$ $x^{\frac{1}{3}} = \frac{-2}{3} \text{ or/of } x^{\frac{1}{3}} = 5$ $x = \frac{-8}{27} \text{ or/of } x = 125$ <p>OR/OF</p>		<ul style="list-style-type: none"> ✓ factors/faktore ✓ $x^{\frac{1}{3}} = \frac{-2}{3}$ or/of $x^{\frac{1}{3}} = 5$ ✓ answer/antwoord

	$3x^{\frac{2}{3}} - 13x^{\frac{1}{3}} - 10 = 0$ <p>Let/stel $x^{\frac{1}{3}} = m$</p> $3m^2 - 13m - 10 = 0$ $(3m + 2)(m - 5) = 0$ $m = \frac{-2}{3} \text{ or/of } m = 5$ $x^{\frac{1}{3}} = \frac{-2}{3} \text{ or/of } x^{\frac{1}{3}} = 5$ $x = \frac{-8}{27} \text{ or/of } x = 125$	<p>✓ factors/faktore</p> <p>✓ $x^{\frac{1}{3}} = \frac{-2}{3}$ or/of $x^{\frac{1}{3}} = 5$</p> <p>✓ answer/antwoord</p> <p>(3)</p>
1.2.1	$2x^2 - 7x - 15 \geq 0$ $(2x + 3)(x - 5) \geq 0$ <p>$x \leq \frac{-3}{2}$ or/of $x \geq 5$</p>  <p>OR/OF</p> $x \in (-\infty; \frac{-3}{2}] \text{ or/of } [5; \infty)$ <p>OR/OF</p>  <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p>Note/Let op:</p> <p>If/As $x \leq \frac{-3}{2}$ and/en $x \geq 5$ max/maks. 3 marks/punte.</p> <p>If/As $x \geq \frac{-3}{2}$ or/of $x \geq 5$ max/ maks. 2 marks/punte.</p> <p>If correct graphical solution but concludes incorrectly, max 3 marks./ As korrekte grafiese oplossing, maar maak verkeerde gevolgtrekking, maks. 3 punte.</p> <p>If omits "or", max 3 marks./ As "of" uitlaat, maks 3 punte.</p> </div>	<p>✓ factors/faktore</p> <p>✓ $\frac{-3}{2}$; 5</p> <p>✓✓ answer/antwoord</p> <p>(4)</p>
1.2.2	$x \geq 5 ; x \neq 8$ <p>OR/OF</p> 	<p>✓ $x \geq 5$</p> <p>✓ $x \neq 8$</p> <p>(2)</p> <p>[15]</p>

QUESTION 2/VRAAG 2

2.1	$4^{x+y} = 2^{y+4}$ $2^{2x+2y} = 2^{y+4}$ $2x + 2y = y + 4$ $y = -2x + 4$ $2x^2 - 3xy = -4$ $2x^2 - 3x(-2x + 4) = -4$ $2x^2 + 6x^2 - 12x + 4 = 0$ $8x^2 - 12x + 4 = 0$ $2x^2 - 3x + 1 = 0$ $(2x - 1)(x - 1) = 0$ $x = \frac{1}{2} \text{ or/of } x = 1$ $y = 3 \text{ or/of } y = 2$ OR/OF $4^{x+y} = 2^{y+4}$ $2^{2x+2y} = 2^{y+4}$ $2x + 2y = y + 4$ $x = \frac{-y}{2} + 2$ $2x^2 - 3xy = -4$ $2\left(\frac{-y}{2} + 2\right)^2 - 3y\left(\frac{-y}{2} + 2\right) = -4$ $\frac{y^2}{2} - 4y + 8 + \frac{3y^2}{2} - 6y = -4$ $4y^2 - 20y + 24 = 0$ $y^2 - 5y + 6 = 0$ $(y - 3)(y - 2) = 0$ $y = 3 \text{ or/of } y = 2$ $x = \frac{1}{2} \text{ or/of } x = 1$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>If a candidate makes a mistake and both equations become linear, max. 3 marks.</p> <p><i>Indien 'n kandidaat 'n fout begaan en beide vergelykings word lineêr, maks. 3 punte.</i></p> </div>	<ul style="list-style-type: none"> ✓ 2^{2x+2y} ✓ $y = -2x + 4$ ✓ substitution/substitusie ✓ standard form/standaardvorm ✓ factors/faktore ✓ x-values/waardes ✓ y-values/waardes ✓ 2^{2x+2y} ✓ $x = \frac{-y}{2} + 2$ ✓ Substitution/substitusie ✓ Standard form/standaardvorm ✓ Factors/faktore ✓ x-values/waardes ✓ y-values/waardes <p style="text-align: right;">(7)</p>
2.2	$b^2 - 4ac = (-5)^2 - 4(3)(3) = -11$ <p>∴ roots are nonreal/wortels is nie-reël</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Note/Let op: If a candidate states 'nonreal' and eg. 'irrational', max 1 mark./</p> <p><i>Indien kandidaat 'nie-reël' en bv. 'irrasionaal' meld, maks 1 punt.</i></p> </div>	<ul style="list-style-type: none"> ✓ -11 ✓ conclusion/gevolgtrekking <p style="text-align: right;">(2)</p> <p style="text-align: right;">[9]</p>

QUESTION 3/VRAAG 3

3.1	$T_4 = 10$	✓ answer/antwoord (1)
3.2	$T_n = an^2 + bn + c$ Second difference/Tweede verskil = -4 $2a = -4$ $a = -2$ $3a + b = 8$ $-6 + b = 8$ $b = 14$ $a + b + c = 2$ $-2 + 14 + c = 2$ $c = -10$ $T_n = -2n^2 + 14n - 10$ OR/OF $T_n = an^2 + bn + c$ $a + b + c = 2$ (1) $4a + 2b + c = 10$ (2) $9a + 3b + c = 14$ (3) $(2) - (1)$ $3a + b = 8$ $(3) - (2)$ $5a + b = 4$ $2a = -4$ $a = -2$ $b = 14$ $c = -10$ $T_n = -2n^2 + 14n - 10$	✓ Second difference/ Tweede verskil ✓ a-value/waarde ✓ b-value/waarde ✓ c-value/waarde ✓ method/metode ✓ a-value/waarde ✓ b-value/waarde ✓ c-value/waarde (4) [5]

QUESTION 4/VRAAG 4

4.1.1	$3 ; \frac{64}{250}$	✓ 3 ✓ $\frac{64}{250}$	(2)
4.1.2	$3 ; \frac{1}{2} ; 3 ; \frac{4}{10} ; 3 ; \frac{16}{50} ; \dots$ 3; 3; 3; ... (18 terms/terme) $\frac{1}{2} ; \frac{4}{10} ; \frac{16}{50} ; \dots$ (GS/MR 17 terms/terme) $S_{35} = 18(3) + \frac{\frac{1}{2}\left(\left(\frac{4}{5}\right)^{17} - 1\right)}{\frac{4}{5} - 1}$ $S_{35} = 54 + 2,44$ $S_{35} = 56,44$	✓ identifies two patterns/ <i>identifiseer twee patrone</i> ✓ substitution/substitusie ✓ 54 ✓ 2,44 ✓ answer/antwoord	(5)
4.2	$T_1 = 5 \cdot 3^{1-3} = 5 \cdot 3^{-2} = \frac{5}{9};$ $T_2 = 5 \cdot 3^{1-4} = 5 \cdot 3^{-3} = \frac{5}{27}$ $a = \frac{5}{9} ; r = \frac{1}{3}$ $S_{\infty} = \frac{a}{1-r}$ $S_{\infty} = \frac{\frac{5}{9}}{1-\frac{1}{3}}$ $S_{\infty} = \frac{5}{6}$ or/of 0,83	<div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> Answer ONLY: 1 mark SLEGS antwoord: 1 punt </div> ✓ a-value/waarde ✓ r-value/waarde <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> If a candidate substitutes incorrect r-value, CA only if $-1 < r < 1$. Indien kandidaat verkeerde r-waarde vervang, CA slegs as $-1 < r < 1$. </div> ✓ substitution/substitusie ✓ answer/antwoord	(4)

[11]

QUESTION 5/VRAAG 5

5.1.1	26; 28; 30	✓ answer/antwoord (1)
5.1.2	<p>26; 28; 30; ...; 998</p> $26 + (n - 1)2 = 998$ $26 + 2n - 2 = 998$ $2n = 974$ $n = 487$ $S_n = \frac{n}{2}[2a + (n - 1)d]$ $S_{487} = \frac{487}{2}[2(26) + 486(2)]$ $S_{487} = 249\,344$ <p>OR/OF</p> <div style="border: 1px solid black; padding: 2px; display: inline-block;"> Answer ONLY: Full marks SLEGS antwoord: Volpunte </div> <p>26; 28; 30; ...; 998</p> $26 + (n - 1)2 = 998$ $26 + 2n - 2 = 998$ $2n = 974$ $n = 487$ $S_n = \frac{n}{2}[a + l]$ $S_{487} = \frac{487}{2}[26 + 998]$ $S_{487} = 249\,344$	<p>✓ $T_n = 998$</p> <p>✓ substitution/substitusie</p> <p>✓ n-value/waarde</p> <p>✓ substitution/substitusie</p> <p>✓ answer/antwoord</p> <p>✓ $T_n = 998$</p> <p>✓ substitution/substitusie</p> <p>✓ n-value/waarde</p> <p>✓ substitution/substitusie</p> <p>✓ answer/antwoord</p> <p>(5)</p>
5.2	$T_m = k \quad \therefore \quad k = a + (m - 1)d$ $T_k = m \quad \therefore \quad m = a + (k - 1)d$ $k = a + md - d \quad \dots \quad (1)$ $m = a + kd - d \quad \dots \quad (2)$ $(1) - (2) \quad \quad \quad k - m = md - kd$ $md - kd = k - m$ $d(m - k) = k - m$ $d = \frac{k - m}{-(k - m)}$ $d = -1$ <div style="border: 1px solid black; padding: 2px; display: inline-block;"> Answer ONLY: 1 mark SLEGS antwoord: 1 punt </div>	<p>✓ substitution/substitusie</p> <p>✓ simultaneous equation/ gelyktydige vergelykings</p> <p>✓ factors/faktore</p> <p>✓ answer/antwoord</p> <p>(4)</p> <p>[10]</p>

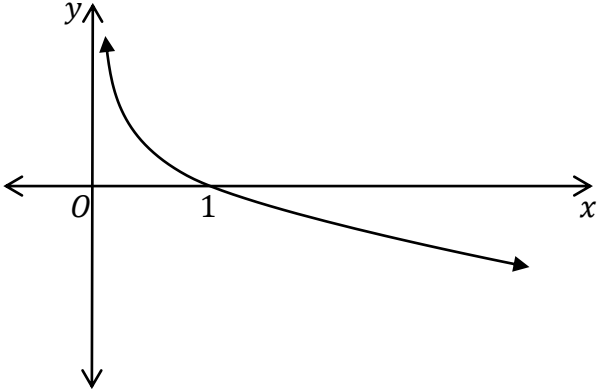
QUESTION 6/VRAAG 6

6.1	$A = P(1 - i)^n$ $83\,543 = 245\,000(1 - 0,13)^n$ $(0,34 \dots) = 0,87^n$ $\log(0,87)^n = \log(0,34 \dots)$ <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 5px auto;"> Wrong formula: 0 marks Verkeerde formule: 0 punte </div> $n = \frac{\log(0,34\dots)}{\log(0,87)}$ $n = 7,73 \text{ years/jare}$ <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 5px auto;"> Accept/Aanvaar 7,7 years/jare; 8 years/jare or/of 7 years/jare 9 months/maande </div>	<ul style="list-style-type: none"> ✓ substitution/substitusie ✓ simplification/vereenvoud. ✓ correct use of logs/korrekte gebruik van logs ✓ answer/antwoord <p style="text-align: right;">(4)</p>
6.2.1	$\frac{10}{100} \times 450\,000 = R45\,000$ $\therefore \text{Loan amount/Leningsbedrag} = R405\,000$ <p>OR/OF</p> $\text{Loan amount/Leningsbedrag}$ $\frac{90}{100} \times 450\,000 = R405\,000$	<ul style="list-style-type: none"> ✓ R45 000 ✓ answer/antwoord ✓ $\frac{90}{100} \times 450\,000$ ✓ R405 000 <p style="text-align: right;">(2)</p>
6.2.2	$P = \frac{x[1-(1+i)^{-n}]}{i}$ $405\,000 = \frac{x\left[1-\left(1+\frac{0,08}{12}\right)^{-240}\right]}{\frac{0,08}{12}}$ $x = R3\,387,58$ <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 5px auto;"> Wrong formula: max 1 mark (i) Verkeerde formule: maks. 1 punt (i) </div>	<ul style="list-style-type: none"> ✓ i ✓ correct formula/formule ✓ substitution/substitusie ✓ answer/antwoord <p style="text-align: right;">(4)</p>
6.2.3	$\text{Balance/balans} = \frac{x[1-(1+i)^{-n}]}{i}$ $= \frac{3\,387,58\left[1-\left(1+\frac{0,08}{12}\right)^{-36}\right]}{\frac{0,08}{12}}$ $= R108\,103,79$ <p>OR/OF</p> <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 5px auto;"> If no rounding from 6.2.2 balance = R108 103,87 Indien geen afronding uit 6.2.2 balans = R108 103,87 </div> $\text{Bal.} = 405\,000\left(1 + \frac{0,08}{12}\right)^{204} - \frac{3\,387,58\left[\left(1 + \frac{0,08}{12}\right)^{204} - 1\right]}{\frac{0,08}{12}}$ $= R108\,104,85$	<ul style="list-style-type: none"> ✓ method/metode ✓ substitution/substitusie ✓ answer/antwoord <p style="text-align: right;">(3) [13]</p>

QUESTION 7/VRAAG 7

7.1.1	$f(x) = \frac{2}{x+5} - 2$	<ul style="list-style-type: none"> ✓ +5 ✓ -2 	(2)
7.1.2	Let/stel $x = 0$ $y = \frac{2}{5} - 2 = -1\frac{3}{5}$ $(0; -1\frac{3}{5})$ OR/OF $(0; \frac{-8}{5})$ OR/OF $(0; -1,6)$	<ul style="list-style-type: none"> ✓ $x = 0$ ✓ $-1\frac{3}{5}$ 	(2)
7.1.3	$y = mx - \frac{8}{5}$ $(-5; -2)$ $-2 = -5m - \frac{8}{5}$ $-10 = -25m - 8$ $25m = 2$ $m = \frac{2}{25}$ $y = \frac{2}{25}x - \frac{8}{5}$ OR/OF $(-5; -2), (0; -1\frac{3}{5})$ $m = \frac{-2 - (-\frac{8}{5})}{-5} = \frac{2}{25}$ $y = \frac{2}{25}x - \frac{8}{5}$	<ul style="list-style-type: none"> ✓ $c = -\frac{8}{5}$ ✓ substitution/substitusie $(-5; -2)$ ✓ m-value/waarde ✓ equation/vergelyking ✓ substitution/substitusie A and B ✓ m-value/waarde ✓ $c = -\frac{8}{5}$ ✓ equation/vergelyking 	(4)
7.1.4	$\frac{2}{x+5} - 2 = \frac{2}{25}x - \frac{8}{5}$ $\times 25(x+5)$ $50 - 50x - 250 = 2x^2 + 10x - 40x - 200$ $2x^2 + 20x = 0$ $2x(x+10) = 0$ $x = 0$ or/of $x = -10$ $\therefore (-10; -2\frac{2}{5})$	<ul style="list-style-type: none"> ✓ setting up equation/opstel van vergelyking ✓ standard form/standaardvorm ✓ factors/faktore ✓ answer/antwoord 	(4)

Answer ONLY: Full marks
 SLEGS antwoord: Volpunte

7.2.1	Decreasing function/ <i>afnemende funksie</i> <i>y</i> decreases as <i>x</i> increases/ <i>y neem af soos wat x toeneem.</i>	✓ decreasing/ <i>afnemend</i> ✓ reason/ <i>rede</i> (2)
If sketch is given as reason: Max 1 mark As skets as rede gegee is: Maks 1 punt		
7.2.2	$y > -2$	✓ answer/ <i>antwoord</i> (1)
7.2.3	$y = \left(\frac{1}{5}\right)^x$ $x = \left(\frac{1}{5}\right)^y$ <i>y</i> = $\log_{\frac{1}{5}}x$ OR/OF <i>y</i> = $-\log_5x$ OR/OF <i>y</i> = $\frac{-\log x}{\log 5}$	✓ interchange <i>x</i> and <i>y</i> <i>ruil x en y</i> ✓ equation/ <i>vergelyking</i> (2)
7.2.4		✓ <i>x</i> -intercept/ <i>x-afsnit</i> ✓ shape/ <i>vorm</i> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> Do not award shape-mark if graph is not asymptotic. <i>Moenie vormpunt toeken as grafiek nie asimptoties is nie.</i> </div> (2)
7.2.5	$0 < x \leq 5$	✓ $x > 0$ ✓ $x \leq 5$ (2) [21]

QUESTION 8/VRAAG 8

8.1	$-x^2 - x + 12 = 0$ $x^2 + x - 12 = 0$ $(x + 4)(x - 3) = 0$ $x = -4 \text{ or/of } x = 3$	✓ $f(x) = 0$ ✓ factors/faktore ✓ both/albei x (3)
8.2	$x = \frac{-b}{2a} = \frac{-(-1)}{2(-1)} = \frac{-1}{2}$ $f\left(\frac{-1}{2}\right) = -\left(\frac{-1}{2}\right)^2 - \left(\frac{-1}{2}\right) + 12 = 12\frac{1}{4}$ <p>OR/OF</p> $x = \frac{-4+3}{2} = \frac{-1}{2}$ $f\left(\frac{-1}{2}\right) = -\left(\frac{-1}{2}\right)^2 - \left(\frac{-1}{2}\right) + 12 = 12\frac{1}{4}$ <p>OR/OF</p> $f'(x) = -2x - 1 = 0$ $x = \frac{-1}{2}$ $f\left(\frac{-1}{2}\right) = -\left(\frac{-1}{2}\right)^2 - \left(\frac{-1}{2}\right) + 12 = 12\frac{1}{4}$ <p>OR/OF</p> $x = \frac{-1}{2}$ $y = \frac{4ac-b^2}{4a}$ $= \frac{4(-1)(12)-(-1)^2}{4(-1)}$ $= \frac{49}{4} \text{ or/of } 12\frac{1}{4}$	✓ x -value/waarde ✓ y -value/waarde ✓ x -value/waarde ✓ y -value/waarde ✓ x -value/waarde ✓ y -value/waarde ✓ x -value/waarde ✓ y -value/waarde (2)
8.3	$-x^2 - x + 12 - (x + 4) = \frac{27}{4}$ $-x^2 - 2x + 8 = \frac{27}{4}$ $-4x^2 - 8x + 32 = 27$ $4x^2 + 8x - 5 = 0$ $(2x - 1)(2x + 5) = 0$ $x = \frac{1}{2} \text{ or/of } x = \frac{-5}{2}$ $M\left(\frac{-5}{2}; 0\right)$	✓ setting up equation/opstel van vergelyking ✓ standard form/standaardvorm ✓ factors/faktore ✓ answer/antwoord (4)

8.4	$x < -4$ or/of $0 < x < 3$	$\checkmark x < -4$ $\checkmark 0 < x < 3$ (2)
8.5	$-x^2 - x + 12 = k$ $-x^2 - x + 12 - k = 0$ $\frac{-1}{4} < 12 - k < 0$ $-12\frac{1}{4} < -k < -12$ $12 < k < 12\frac{1}{4}$	$\checkmark \frac{-1}{4} < 12 - k < 0$ $\checkmark 12 < k < 12\frac{1}{4}$ (2)
8.6	$h(x) = -\left(x - 2\frac{1}{2}\right)^2 + 12\frac{1}{4}$	$\checkmark -\left(x - 2\frac{1}{2}\right)^2$ $\checkmark 12\frac{1}{4}$ (2) [15]

QUESTION 9/VRAAG 9

<p>9.1</p>	$f(x) = -5x^2 + 2x$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{-5(x+h)^2 + 2(x+h) - (-5x^2 + 2x)}{h}$ $= \lim_{h \rightarrow 0} \frac{-5(x^2 + 2xh + h^2) + 2x + 2h + 5x^2 - 2x}{h}$ $= \lim_{h \rightarrow 0} \frac{-5x^2 - 10xh - 5h^2 + 2x + 2h + 5x^2 - 2x}{h}$ $= \lim_{h \rightarrow 0} \frac{-10xh - 5h^2 + 2h}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-10x - 5h + 2)}{h}$ $= \lim_{h \rightarrow 0} (-10x - 5h + 2)$ $= -10x + 2$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> Answer ONLY: 0 marks SLEGS antwoord: 0 punte </div> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> Penalise 1 mark for incorrect use of formula. Must show $f'(x)$. Penaliseer 1 punt vir verkeerde gebruik van formule. Moet $f'(x)$ toon. </div>	<ul style="list-style-type: none"> ✓ formula/formule ✓ substitution of/substitusie van $(x + h)$ ✓ simplification to/vereenvoudiging na $(-10xh - 5h^2 + 2h)$ ✓ common factor/gemene faktor ✓ answer/antwoord <p style="text-align: right;">(5)</p>
<p>9.2</p>	$y = \frac{8}{x^4} + \sqrt[3]{x^2}$ $y = 8x^{-4} + x^{\frac{2}{3}}$ $\frac{dy}{dx} = -32x^{-5} + \frac{2}{3}x^{-\frac{1}{3}}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> Penalise 1 mark for incorrect notation. Penaliseer 1 punt vir verkeerde notasie. </div>	<ul style="list-style-type: none"> ✓ $8x^{-4}$ ✓ $x^{\frac{2}{3}}$ ✓ $-32x^{-5}$ ✓ $\frac{2}{3}x^{-\frac{1}{3}}$ <p style="text-align: right;">(4)</p>
<p>9.3</p>	$f(x) = -x^3 + 3x - 2$ $f'(x) = -3x^2 + 3 = \frac{8}{3}$ $-9x^2 + 9 = 8$ $9x^2 - 1 = 0$ $(3x - 1)(3x + 1) = 0$ $x = \frac{1}{3} \text{ or/of } x = -\frac{1}{3}$	<ul style="list-style-type: none"> ✓ $f'(x)$ ✓ $f'(x) = \frac{8}{3}$ ✓ standard form/standaardvorm ✓ factors/faktore ✓ answer/antwoord <p style="text-align: right;">(5)</p> <p style="text-align: right;">[14]</p>

QUESTION 10/VRAAG 10

10.1.1	$f(x) = x^3 - 5x^2 - 8x + 12$ $(x - 6)(x^2 + x - 2) = 0$ $(x - 6)(x + 2)(x - 1) = 0$ $x = 6$ or/of $x = -2$ or/of $x = 1$ $A(-2; 0)$ and/en $B(1; 0)$	$\checkmark (x - 6)$ $\checkmark (x^2 + x - 2)$ $\checkmark (x + 2)(x - 1)$ \checkmark coordinates of A and B/ <i>koördinate van A en B</i>	(4)
10.1.2	$f'(x) = 3x^2 - 10x - 8 = 0$ $(3x + 2)(x - 4) = 0$ $x = -\frac{2}{3}$ or/of $x = 4$ $D\left(-\frac{2}{3}; 14\frac{22}{27}\right)$ and/en $E(4; -36)$	$\checkmark f'(x)$ $\checkmark f'(x) = 0$ \checkmark factors/ <i>faktore</i> \checkmark D coordinates/ <i>koördinate</i> \checkmark E coordinates/ <i>koördinate</i>	(5)
10.2.1	$f(2) = 0$ $\therefore g(0) = -5$ OR/OF $f'(x) = 3ax^2 + 2bx - 5$ $f'(0) = -5$	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 0 auto;"> Answer ONLY: Full marks SLEGS antwoord: Volpunte </div> $\checkmark f(2) = 0$ $\checkmark g(0) = -5$ $\checkmark f'(x) = 3ax^2 + 2bx - 5$ $\checkmark f'(0) = -5$	(2)
10.2.2	$m = \frac{50-0}{0-(-5)} = 10$	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 0 auto;"> Answer ONLY: Full marks SLEGS antwoord: Volpunte </div> $\checkmark \frac{50-0}{0-(-5)}$ \checkmark answer/ <i>antwoord</i>	(2)
10.2.3	Point of inflection/ <i>Infleksiepunt</i> at/by $x = -2\frac{2}{3}$ $f''(x) < 0$ if/as $x > -2\frac{2}{3}$	$\checkmark x = -2\frac{2}{3}$ \checkmark answer/ <i>antwoord</i>	(2)
<div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 0 auto;"> Answer ONLY: Full marks SLEGS antwoord: Volpunte </div>			[15]

QUESTION 11/VRAAG 11

11.1	$SP = \sqrt{2x^2} = \sqrt{2}x$ $LP = LQ = (50 - x)$ $PQ^2 = (50 - x)^2 + (50 - x)^2$ $= 2(50 - x)^2$ $PQ = \sqrt{2}(50 - x)$ $A = \sqrt{2}(50 - x) \times \sqrt{2}x$ $= 2x(50 - x)$ $= 100x - 2x^2$	$\checkmark SP = \sqrt{2x^2}$ $\checkmark PQ^2 = (50 - x)^2 + (50 - x)^2$ $\checkmark PQ = \sqrt{2}(50 - x)$ $\checkmark A = 2x(50 - x)$	(4)
11.2	$\frac{dA}{dx} = 100 - 4x = 0$	$\checkmark 100 - 4x = 0$	

	$-4x = -100$ $x = 25$ $A = 100(25) - 2(25)^2$ $= 1\,250\text{ cm}^2$	✓ <i>x</i> -value/waarde ✓ answer/antwoord (3) [7]
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QUESTION 12/VRAAG 12

12.1.1	$x = 8$	✓ answer/antwoord (1)
12.1.2	$y = 13$ <div style="border: 1px solid black; padding: 2px; display: inline-block; margin-left: 20px;"> If incorrect <i>x</i>-value/Indien verkeerde <i>x</i>-waarde: CA: $y = x + 5$ </div>	✓ answer/antwoord (1)
12.2.1	$P(\text{first client takes a loaf of white bread}) = \frac{7}{12}$ $P(\text{eerste kliënt vat 'n witbrood}) = \frac{7}{12}$	✓ answer/antwoord (1)
12.2.2	$P(BB) = \frac{5}{12} \times \frac{4}{11}$ $= \frac{20}{132}$ or/of $\frac{5}{33}$	✓ $\frac{5}{12}$ ✓ $\frac{4}{11}$ ✓ $\frac{20}{132}$ or/of $\frac{5}{33}$ (3)
12.2.3	<p style="text-align: center;"> $P(WB)$ or/of $P(BW) = \left(\frac{7}{12} \times \frac{6}{12}\right) + \left(\frac{5}{12} \times \frac{8}{12}\right)$ $= \frac{41}{72}$ or/of 0,57 </p>	✓ $\left(\frac{7}{12} \times \frac{6}{12}\right)$ ✓ $\left(\frac{5}{12} \times \frac{8}{12}\right)$ ✓ answer/antwoord (3)

12.3.1	$9! = 362\,880$	✓ answer/antwoord (1)
12.3.2	$n(\text{E's next to each other}/E's \text{ langs mekaar})$ $= 8 \times 7! \times 2$ $= 80\,640$ $P(\text{E's next to each other}/E's \text{ langs mekaar})$ $= \frac{80\,640}{362\,880} \text{ or/of } \frac{2}{9}$	✓ $8 \times 7! \times 2$ ✓ $80\,640$ ✓ $\frac{80\,640}{362\,880} \text{ or/of } \frac{2}{9}$ (3)
12.3.3	$n(\text{starting with } P; \text{ repeating letters the same})$ $n(\text{begin met } P; \text{ herhaalde letters dieselfde})$ $= \frac{8!}{2!2!}$ $= 10\,080$	✓ $\frac{8!}{2!2!}$ ✓ $10\,080$ (2) [15]
		TOTAL/TOTAAL: 150