



GAUTENG PROVINCE

EDUCATION
REPUBLIC OF SOUTH AFRICA

PREPARATORY EXAMINATION *VOORBEREIDENDE EKSAMEN*

2017

MEMORANDUM /

NASIEN RIGLYNE

**MATHEMATICS (SECOND PAPER) (10612)
*WISKUNDE (TWEEDE VRAESTEL) (10612)***

19 pages / bladsye

GAUTENG DEPARTMENT OF EDUCATION /
GAUTENGSE DEPARTEMENT VAN ONDERWYS
PREPARATORY EXAMINATION /
VOORBEREIDENDE EKSAMEN

MATHEMATICS / WISKUNDE
(Second Paper / Tweede Vraestel)

MEMORANDUM

QUESTION/VRAAG 1

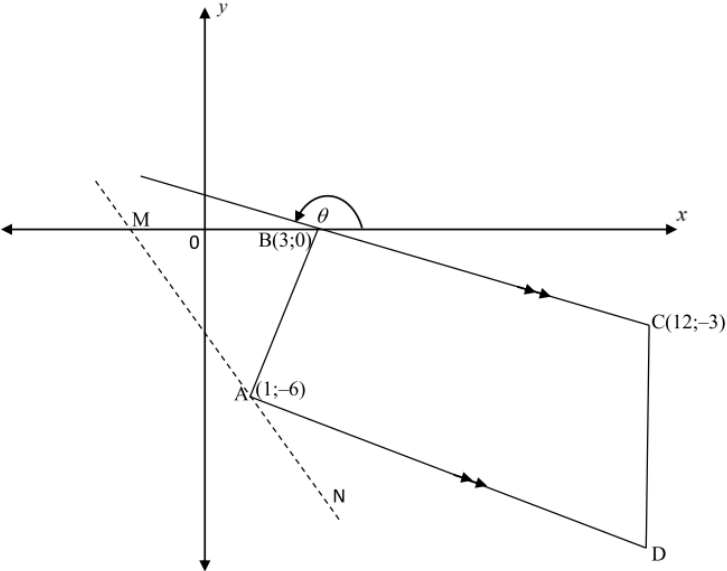
1.1		
1.1.1	median / <i>mediaan</i> = 55	✓ 55 (1)
1.1.2	IQR/ <i>IKV</i> = 60 – 40 = 20	✓ 60 – 40 ✓ 20 (2)
1.1.3	15% – 65%	✓ 15% – 65% (1)
1.1.4	Skewed to the left / <i>Skeef na links</i> OR Negatively skewed / <i>Negatief skeef</i>	✓ answer/ <i>antwoord</i> (1)

<p>1.2</p>	<table border="1"> <thead> <tr> <th>Class interval / <i>Klasinterval</i></th> <th>Cumulative Frequency / <i>Kumulatiewe Frekwensie</i></th> </tr> </thead> <tbody> <tr> <td>$10 \leq x \leq 19$</td> <td>1</td> </tr> <tr> <td>$20 \leq x \leq 29$</td> <td>2</td> </tr> <tr> <td>$30 \leq x \leq 39$</td> <td>4</td> </tr> <tr> <td>$40 \leq x \leq 49$</td> <td>6</td> </tr> <tr> <td>$50 \leq x \leq 59$</td> <td>14</td> </tr> <tr> <td>$60 \leq x \leq 69$</td> <td>19</td> </tr> <tr> <td>$70 \leq x \leq 79$</td> <td>23</td> </tr> <tr> <td>$80 \leq x \leq 89$</td> <td>26</td> </tr> <tr> <td>$90 \leq x \leq 100$</td> <td>30</td> </tr> </tbody> </table>	Class interval / <i>Klasinterval</i>	Cumulative Frequency / <i>Kumulatiewe Frekwensie</i>	$10 \leq x \leq 19$	1	$20 \leq x \leq 29$	2	$30 \leq x \leq 39$	4	$40 \leq x \leq 49$	6	$50 \leq x \leq 59$	14	$60 \leq x \leq 69$	19	$70 \leq x \leq 79$	23	$80 \leq x \leq 89$	26	$90 \leq x \leq 100$	30	
Class interval / <i>Klasinterval</i>	Cumulative Frequency / <i>Kumulatiewe Frekwensie</i>																					
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$90 \leq x \leq 100$	30																					
<p>1.2.1</p>	<p style="text-align: center;"><i>Ogive / Ogief</i></p>	<ul style="list-style-type: none"> ✓ top points of interval / <i>hoogte punt van interval</i> ✓ shape / <i>vorm</i> ✓ grounding point / <i>laagste punt</i> <p style="text-align: right;">(3)</p>																				
<p>1.2.2</p>	$\frac{19}{30} \times 100$ $= 63\%$	<ul style="list-style-type: none"> ✓ 63% (accuracy / <i>akkuraatheid</i>) <p style="text-align: right;">(1)</p>																				
<p>1.2.3</p>	$26 - 23$ $= 3 \text{ learners/leerders}$	<ul style="list-style-type: none"> ✓ 3 <p style="text-align: right;">(1)</p>																				
<p>1.2.4</p>	<p>Mark between 30 – 39/<i>Enige punt tussen 30 – 39</i></p>	<ul style="list-style-type: none"> ✓ 30 – 39 <p style="text-align: right;">(1)</p>																				
<p>1.2.5</p>	$90 - 19$ $= 71$	<ul style="list-style-type: none"> ✓ 71 <p style="text-align: right;">(1)</p>																				
<p>[12]</p>																						

QUESTION/VRAAG 2

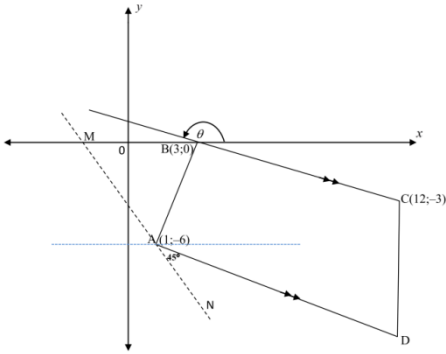
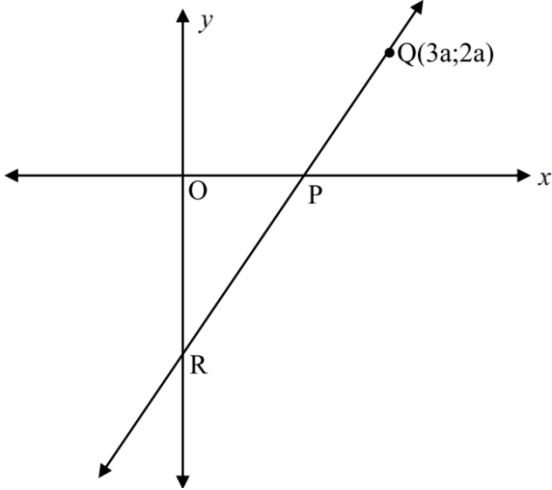
2.1	$\hat{y} = 0,84x - 2,92$	✓ $a = 0,84x$ ✓ $b = -2,92$ ✓ equation / vergelyking (3)
2.2	$r = 0,95$	✓ $r = 0,95$ (1)
2.3	<p style="text-align: center;">Paper 1 / Vraestel 2</p>	line through the point: / lyn deur die punte: ✓ (46;36) average point / gemiddelde punt ✓ (3,5 ; 0) x -intercept / x -afsnit (2)
2.4	$y = 0,84(98) - 2,92$ $y = 79,4$ OR / OF calculator / optel masjien Yes / agree The correlation suggests a positive association between variables, therefore predictions using the least squares regression line is valid, reliable and usually accurate. Ja / stem saam Die korrelasie dui op 'n positiewe assosiasie tussen veranderlikes, daarom is voorspellings met behulp van die kleinste kwadrate regressielyn geldig, betroubaar en gewoonlik akkuraat.	✓ yes / ja ✓ reason / rede (2)
		[8]

QUESTION/VRAAG 3

3.1		
3.1.1	$m_{BC} = \frac{-3-0}{12-3}$ $= -\frac{1}{3}$ $\tan \theta = m_{BC}$ $= -\frac{1}{3}$ $\theta = 180^\circ - 18,43^\circ$ $= 161,57^\circ$	$\checkmark m_{BC} = -\frac{1}{3}$ $\checkmark \tan \theta = -\frac{1}{3}$ $\checkmark 18,43^\circ$ $\checkmark \theta = 161,57^\circ$
3.1.2	$m_{AD} = m_{BC} \quad \text{AD parallel BC}$ $= -\frac{1}{3}$ $m_{AB} = \frac{-6-0}{1-3}$ $= 3$ $m_{AB} \cdot m_{AD} = 3 \cdot \left(-\frac{1}{3}\right)$ $= -1$ $\therefore AB \perp AD$	$\checkmark m_{AD} = -\frac{1}{3}$ $\checkmark m_{AB} = 3$ $\checkmark m_{AB} \cdot m_{AD} = 3 \cdot \left(-\frac{1}{3}\right)$

(4)

(3)

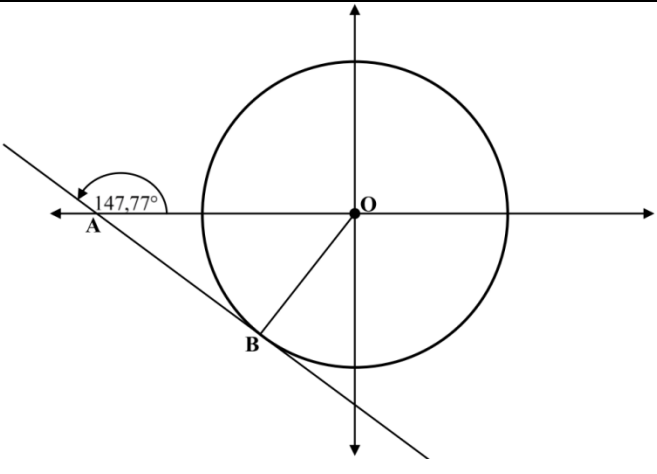
<p>3.1.3</p>	<p>Inclination of the line / <i>Inklinasie van die lyn</i> $\alpha = 161,6^\circ - 45^\circ$ $= 116,6^\circ$ $\tan \alpha = m_{line}$ $\tan 116,6^\circ = -2$ $y - y_1 = m(x - x_1)$ OR/OF $y = mx + q$ $y + 6 = -2(x - 1)$ $-6 = -2(1) + q$ $y + 6 = -2x + 2$ $q = -4$ $y = -2x - 4$</p> 	<p>✓ $\alpha = 116,6^\circ$ ✓ $m = -2$ ✓ substitute / <i>vervang</i> A(1;-6) ✓ $y = -2x - 4$ (4)</p>
<p>3.2</p>		
<p>3.2.1</p>	<p>$y - y_1 = m(x - x_1)$ $y - 2a = 2(x - 3a)$ $y = 2x - 6a + 2a$ $y = 2x - 4a$</p>	<p>✓ substitute / <i>vervang</i> (3a;2a) and / <i>en</i> $m = 2$ ✓ $y = 2x - 4a$ (2)</p>
<p>3.2.2</p>	<p>P(2a;0) Q(0;-4a) Area / <i>Oppervlakte</i> $\Delta POQ = \frac{1}{2} b.h$ $= \frac{1}{2} (2a)(4a)$ $= 4a^2$</p>	<p>✓ P(2a;0) ✓ Q(0;-4a) ✓ correct substitution / <i>korrekte</i> <i>vervanging</i> ✓ $4a^2$ (4)</p>

<p>3.2.3</p>	$m_{DE} = m_{EQ}$ $\frac{-2+14}{3+3} = \frac{2a+2}{3a-3}$ $2(3a-3) = 2a+2$ $6a-6 = 2a+2$ $4a = 8$ $a = 2$ <p>OR / OF</p> $m_{DQ} = m_{DE}$ $\frac{2a+14}{3a+3} = \frac{-2+14}{3+3}$ $2(3a+3) = 2a+14$ $6a+6 = 2a+14$ $4a = 8$ $a = 2$ $m_{DQ} = m_{EQ}$ $\frac{2a+14}{3a+3} = \frac{2a+2}{3a-3}$ $(2a+14)(3a-3) = (2a+2)(3a+3)$ $6a^2 + 36a - 42 = 4a^2 + 12a + 6$ $2a^2 + 24a - 48 = 0$ $a^2 + 12a - 24 = 0$ $(a+12)(a-2) = 0$ $a = -12 \text{ or / of } a = 2$ <p>invalid / ongeldig</p>	$\checkmark \frac{-2+14}{3+3} = \frac{2a+2}{3a-3}$ <p>✓ simplification / vereenvoudiging</p> <p>✓ $a = 2$ (3)</p> $\checkmark \frac{2a+14}{3a+3} = \frac{-2+14}{3+3}$ <p>✓ simplification / vereenvoudiging</p> <p>✓ $a = 2$ (3)</p> $\checkmark \frac{2a+14}{3a+3} = \frac{2a+2}{3a-3}$ <p>✓ simplification / vereenvoudiging</p> <p>✓ $a = 2$ chosen / gekies (3)</p> <p>[20]</p>
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If learner assumed that D and E lie on the straight line QPR do not award any marks. /
 Indien leerder aanvaar het dat D en E op die reguit lyn QPR lê, moet daar geen punte toegeken word nie.

OR/OF

QUESTION/VRAAG 4

4.1		
4.1.1	$x^2 + y^2 = 64$ OR / OF $x^2 + y^2 = 8^2$	$\checkmark x^2 + y^2 = 64$ OR / OF $x^2 + y^2 = 8^2$ (1)
4.1.2	$\hat{OAB} = 32,23^\circ$ (\angle s on a str line / \angle^e op reguit lyn) $\hat{OBA} = 90^\circ$ (tan \perp radius OR tan \perp diameter / raaklyn \perp radius) $\sin 32,23^\circ = \frac{OB}{OA}$ $\sin 32,23^\circ = \frac{8}{OA}$ $OA = \frac{8}{\sin 32,23^\circ}$ $= 15$ $\therefore A(-15;0)$	$\checkmark \hat{OAB} = 32,23^\circ$ $\checkmark \sin 32,23^\circ = \frac{8}{OA}$ $\checkmark OA = 15$ $\checkmark A(-15;0)$ (4)

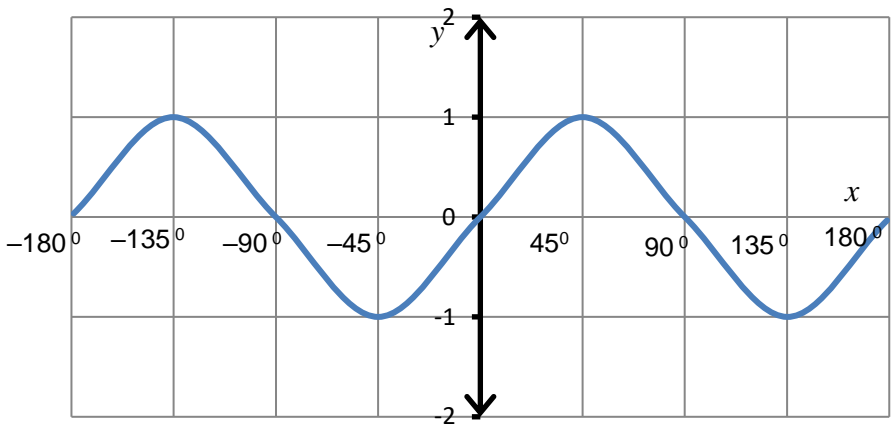
<p>4.2</p>		
<p>4.2.1</p>	$x^2 - 10x + y^2 + 8y + 31 = 0$ $(x - 5)^2 + (y + 4)^2 = -31 + 25 + 16$ $(x - 5)^2 + (y + 4)^2 = -31 + 25 + 16$ $(x - 5)^2 + (y + 4)^2 = 10$	<p>✓ $(x - 5)^2 + (y + 4)^2$ ✓ $- 31 + 25 + 16$ ✓ $(x - 5)^2 + (y + 4)^2 = 10$</p> <p>(3)</p>
<p>4.2.2</p>	<p>A(5; -4)</p>	<p>✓ A(5; -4)</p> <p>(1)</p>
<p>4.2.3</p>	$r^2 = 10$ $r = \sqrt{10}$	<p>✓ $r = \sqrt{10}$</p> <p>(1)</p>
<p>4.2.4</p>	$\frac{x_B + 5}{2} = 2 \quad \text{and/en} \quad \frac{y_B - 4}{2} = -3$ $x_B = -1 \quad y_B = -2$ <p>∴ B(-1; -2)</p>	<p>✓ $\frac{x_B + 5}{2} = 2$ ✓ $\frac{y_B - 4}{2} = -3$ ✓ B(-1; -2)</p> <p>(3)</p>
<p>4.2.5</p>	<p>$k = 5 - \sqrt{10}$ or / of $k = 5 + \sqrt{10}$</p> <div style="border: 1px solid black; padding: 5px; margin: 5px 0;"> Any one of the two can be written first and then be allocated the two marks. / <i>Enigeen van die twee kan eerste geskryf word en dan die twee punte toegeken word.</i> </div>	<p>✓✓ $k = 5 + \sqrt{10}$ ✓ $k = 5 - \sqrt{10}$</p> <p>(3)</p>
<p>4.2.6</p>	$r^2 = AF^2 = 10$ $AD = \sqrt{(11 - 5)^2 + (-6 + 4)^2}$ $= \sqrt{36 + 4}$ $= \sqrt{40}$ $= 2\sqrt{10}$ <p>∠FAD = 90° (radius ⊥ tangent / raaklyn ⊥ radius)</p> <p>FD² = AD² - AF² (Pythagoras)</p> $= (\sqrt{40})^2 - (\sqrt{10})^2$ $= 30$ $FD = \sqrt{30}$	<p>✓ AF² = 10 ✓ substitute in distance formula / <i>vervanging in afstandsformule</i> ✓ AD = $\sqrt{40}$ or $2\sqrt{10}$ ✓ FD = $\sqrt{30}$</p> <p>(4)</p>
<p>[20]</p>		

QUESTION/VRAAG 5

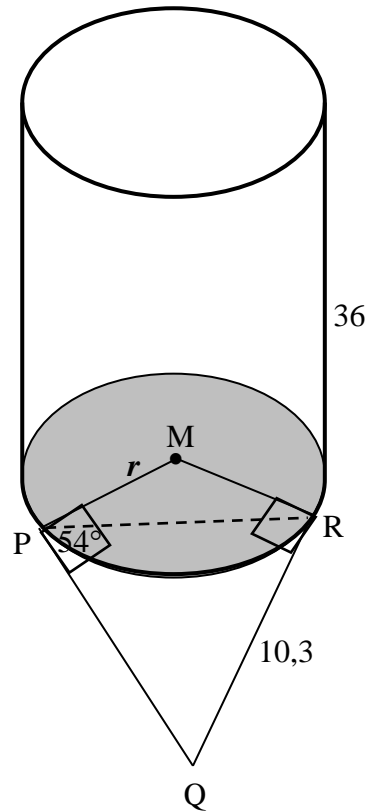
5.1	$\tan \theta = -\frac{1}{4}$ $\hat{O}_1 = 14,04^\circ$ $\theta = 360^\circ - 14,04^\circ$ $= 345,96^\circ$	$\checkmark \tan \theta = -\frac{1}{4}$ $\checkmark \hat{O}_1 = 14,04^\circ$ $\checkmark 345,96^\circ$ <p style="text-align: right;">(3)</p>
5.2	$\frac{2 \cos(90^\circ - x)}{\sin(180^\circ - 2x)} \times \frac{\cos(60^\circ - x) \cos x - \sin(60^\circ - x) \sin x}{\tan(-x)}$ $= \frac{2 \sin x}{\sin 2x} \times \frac{\cos(60^\circ - x + x)}{-\tan x}$ $= \frac{2 \sin x}{2 \sin x \cos x} \times \frac{\cos 60^\circ}{-\frac{\sin x}{\cos x}}$ $= \frac{1}{\cos x} \times \frac{1}{2} \times -\frac{\cos x}{\sin x}$ $= -\frac{1}{2 \sin x}$	$\checkmark 2 \sin x$ $\checkmark \cos(60^\circ - x + x)$ $\checkmark \sin 2x$ $\checkmark -\tan x$ $\checkmark 2 \sin x \cos x$ $\checkmark \frac{\sin x}{\cos x}$ $\checkmark -\frac{1}{2 \sin x}$ <p style="text-align: right;">(7)</p>
5.3.1	$\sin 108^\circ = \sin(90^\circ + 18^\circ)$ $= \cos 18^\circ$ $= k$	$\checkmark \text{reduction/}$ herleiding $\checkmark k$ <p style="text-align: right;">(2)</p>
5.3.2	$\cos(-36^\circ) = \cos 36^\circ$ $= \cos 2(18^\circ)$ $= 2 \cos^2 18^\circ - 1$ $= 2k^2 - 1$	$\checkmark \cos 36^\circ$ $\checkmark 2 \cos^2 18^\circ - 1$ $\checkmark 2k^2 - 1$ <p style="text-align: right;">(3)</p>
5.4	$2 \sin x \cos x + 2 \sin x + \cos^2 x + \cos x = 0$ $2 \sin x (\cos x + 1) + \cos x (\cos x + 1) = 0$ $(\cos x + 1)(2 \sin x + \cos x) = 0$ $\cos x = -1 \quad \text{or / of} \quad 2 \sin x = -\cos x$ $x = 180^\circ + k \cdot 360^\circ \quad \text{or / of} \quad 2 \tan x = -1$ $\tan x = -\frac{1}{2}$ $x = -26,57^\circ + k \cdot 180^\circ \quad k \in \mathbb{Z}$ <p style="text-align: center;">OR / OF</p> $\text{ref} \angle = 26,57^\circ$ $x = 153,43^\circ + k \cdot 180^\circ \quad k \in \mathbb{Z}$ $x = \{-26,57^\circ ; 153,43^\circ ; 180^\circ\}$	$\checkmark \text{common factor/}$ gemeenskaplike faktor $\checkmark \cos x = -1$ $\checkmark \tan x = -\frac{1}{2}$ $\checkmark 153,4^\circ$ $\checkmark -26,57^\circ$ $\checkmark 180^\circ$ <p style="text-align: right;">(6)</p>

5.5.1	$\tan \theta = \frac{p}{1}$ $p^2 + y^2 = r^2$ $p^2 + 1 = r^2$ $r = \sqrt{p^2 + 1}$ $\sin 2\theta = 2 \sin \theta \cos \theta$ $= 2 \left(\frac{p}{\sqrt{p^2 + 1}} \right) \left(\frac{1}{\sqrt{p^2 + 1}} \right)$ $= \frac{2p}{p^2 + 1}$	$\checkmark r = \sqrt{p^2 + 1}$ $\checkmark 2 \left(\frac{p}{\sqrt{p^2 + 1}} \right) \left(\frac{1}{\sqrt{p^2 + 1}} \right)$ <p style="text-align: right;">(2)</p>
5.5.2	$\frac{(p+1)^2}{p^2 + 1}$ $= \frac{p^2 + 2p + 1}{p^2 + 1}$ $= \frac{2p}{p^2 + 1} + \frac{p^2 + 1}{p^2 + 1}$ $= \sin 2\theta + 1$ <p>Maximum of / <i>Maksimum van</i> $\sin 2\theta$ is 1</p> <p>Maximum of / <i>Maksimum van</i> $\frac{(p+1)^2}{p^2 + 1}$ will be 2</p>	$\checkmark \frac{p^2 + 2p + 1}{p^2 + 1}$ $\checkmark \frac{2p}{p^2 + 1} + \frac{p^2 + 1}{p^2 + 1}$ <p>OR/OF $\sin 2\theta + 1$</p> $\checkmark 2$ <p style="text-align: right;">(3) [26]</p>

QUESTION/VRAAG 6

6.1	$a = 1$ $b = 2$	✓ $a = 1$ ✓✓ $b = 2$ (3)
6.2		✓ x -intercepts/ -afsnit ✓ T/P ✓ shape/vorm (3)
6.3	$x \in (45^\circ ; 135^\circ)$ OR/OF $45^\circ < x < 135^\circ$	✓ critical values / <i>kritiese waardes</i> ✓ correct interval / korrekte interval (2) [8]

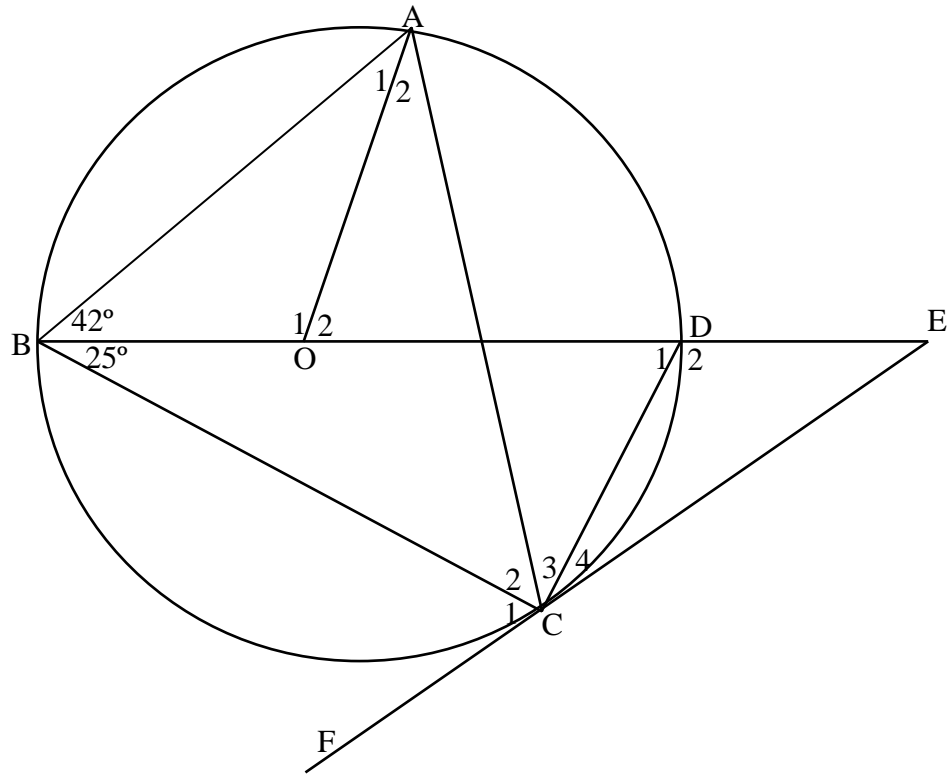
QUESTION/VRAAG 7



7.1	<p>PQ = PR (tangents from the same point / raaklyne vanuit dies. punt)</p> <p>$\hat{P}RQ = 54^\circ$ (\angle's opp. equal sides / \angle° teenoor gelyke sye)</p> <p>$\hat{Q} = 180^\circ - (54^\circ + 54^\circ)$ (\angle's of a Δ / \angle° van Δ)</p> <p>$= 72^\circ$</p>	<p>✓ $\hat{P}RQ = 54^\circ$</p> <p>✓ answer / antwoord (2)</p>
7.2	<p>$PR^2 = (10,3)^2 + (10,3)^2 - 2(10,3)(10,3)\cos 72^\circ$</p> <p>$= 12,11$</p>	<p>✓ substitution into correct cos rule / vervanging na korrekte cos reël</p> <p>✓ answer / antwoord (2)</p>
7.3	<p>MPQR is a cyclic quad. / $MPQR$ is 'n koordevierhoek (opp. \angle's sup)</p> <p>$\therefore \hat{M} = 108^\circ$</p> <p>$(12,11)^2 = r^2 + r^2 - 2(r)(r)\cos 108^\circ$</p> <p>$146,6521 = 2r^2 - 2r^2 \cos 108^\circ$</p> <p>$= 2r^2(1 - \cos 108^\circ)$</p> <p>$r^2 = \frac{146,6521}{2(1 - \cos 108^\circ)}$</p> <p>$= 56,02$</p> <p>Volume of/van silo = $\pi r^2 h$</p> <p>$= \pi(56,02)(36)$</p> <p>$= 6335,71\text{m}^3$</p>	<p>✓ $\hat{M} = 108^\circ$</p> <p>✓ substitution into correct cos rule / vervanging na korrekte cos reël</p> <p>✓ answer / antwoord</p> <p>✓ substitution into correct volume formula/vervanging na korrekte volume formule</p> <p>✓ answer / antwoord (5)</p>

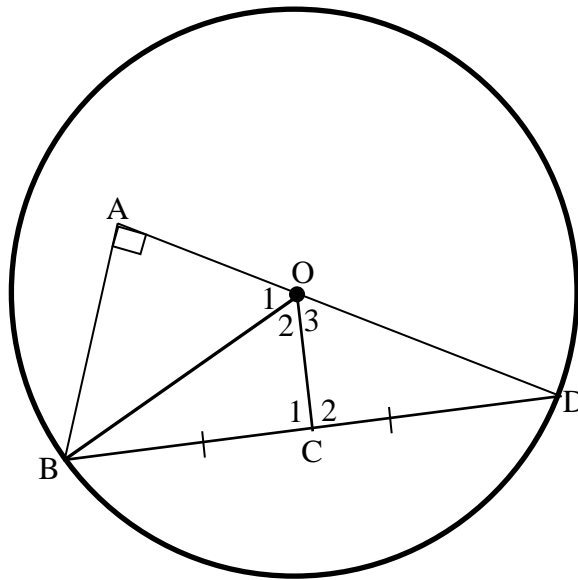
[9]

QUESTION/VRAAG 8



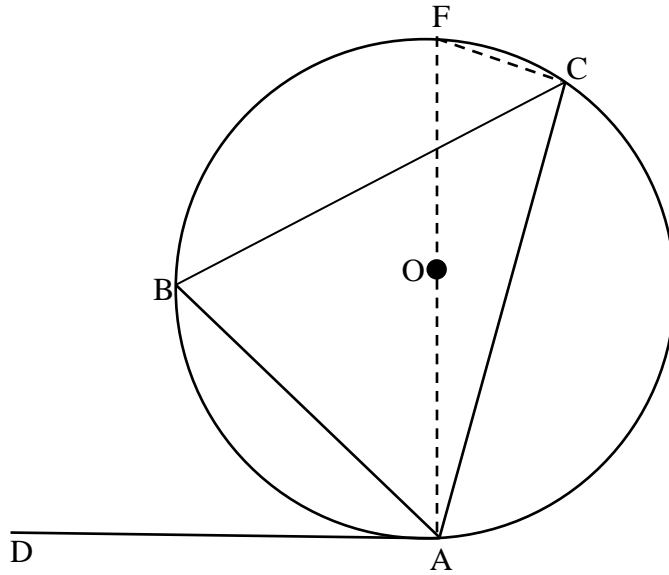
8.1	...centre / ...middelpunt		✓ answer / antwoord (1)
8.2.1	$\hat{BCD} = 90^\circ$	[\angle in semi \odot OR diameter subtends right angle OR \angle in semi \odot OF deursnee onderspan rete hoek OF \angle in $\frac{1}{2} \odot$ / \angle in halwe \odot OF \angle in $\frac{1}{2} \odot$]	✓ $\hat{BCD} = 90^\circ$ ✓R (2)
8.2.2	$\hat{A}_1 = 42^\circ$	[\angle 's opposite equal radii / \angle 's teenoor gelyke radii]	✓ $\hat{A}_1 = 42^\circ$ ✓R (2)
8.2.3	$\hat{O}_2 = 84^\circ$	[\angle at centre = $2 \times \angle$ at circumference / <i>Midpts</i> $\angle = 2 \times$ <i>Omtrek</i> \angle]	✓ $\hat{O}_2 = 84^\circ$ ✓R (2)
8.2.4	$\hat{C}_4 = 25^\circ$	[tan chord theorem / \angle tussen raaklyn en koord]	✓ $\hat{C}_4 = 25^\circ$ ✓R (2) [9]

QUESTION/VRAAG 9



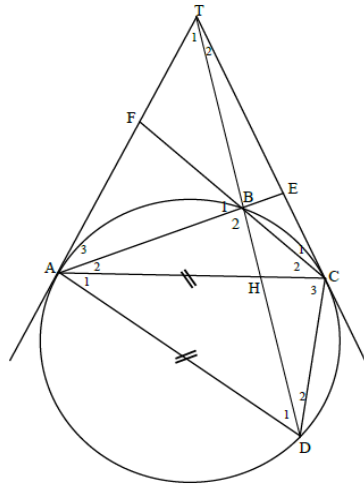
9.1	$DA \cdot OD = OD(OD + OA)$ $= OD^2 + OD \cdot OA$	$\checkmark OD(OD + OA)$ <p style="text-align: right;">(1)</p>
9.2	<p>In $\triangle DA$ and $\triangle DCO$</p> $\hat{D} = \hat{D}$ $\hat{C}_2 = 90^\circ$ $\hat{C}_2 = \hat{A}$ $\hat{B} = \hat{O}_3$ $\therefore \triangle DAB \parallel \triangle DCO \text{ [}\angle\angle\angle\text{]}$ $\therefore \frac{DA}{DC} = \frac{AB}{CO} = \frac{DB}{DO}$ $DA \cdot DO = DC \cdot DB$ $OD^2 + OD \cdot OA = DC \cdot 2DC$ $\therefore OD^2 + OD \cdot OA = 2DC^2$	<p>[common / <i>gemeenskaplik</i>] [line from centre to midpt of chord / <i>Midpt. O ; Midpt. koord</i>] / <i>lyn van middel tot midpunt van koord</i> [3rd \angle^s of \triangle / 3^e \angle^e van \triangle]</p> $\checkmark S \hat{D} = \hat{D}$ $\checkmark S \hat{C}_2 = 90^\circ$ $\checkmark R$ $\checkmark S \hat{C}_2 = \hat{A}$ $\checkmark S \hat{B} = \hat{O}_3$ $\checkmark \frac{DA}{DC} = \frac{AB}{CO} = \frac{DB}{DO}$ $\checkmark OD^2 + OD \cdot OA = DC \cdot 2DC$ <p style="text-align: right;">(7) [8]</p>

QUESTION/VRAAG 10



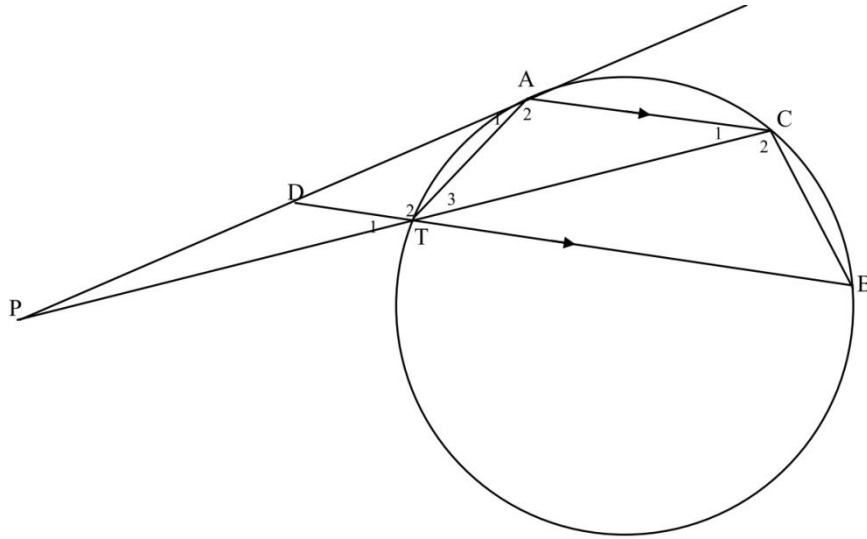
NB No construction: Breakdown 0/5

10. 1	<p>Construction: Draw diameter AOF and join FC</p> <p>Konstruksie: Teken middellyn AOF en verbind FC</p> <p>$\hat{D}AF = 90^\circ$</p> <p>$\hat{F}CA = 90^\circ$</p> <p>$\hat{F}AB = \hat{F}CB$</p> <p>$\hat{D}AB = \hat{B}CA$</p>	<p>✓ Construction on sketch/ Konstruksie op skets</p> <p>✓ S ✓ R</p> <p>✓ R</p> <p>✓ R</p> <p>(5)</p>
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<p>10.2.1</p>	$\hat{D} = \hat{C}_3$ $\hat{D} = \hat{B}_1$ $\hat{C}_3 = \hat{B}_2$ $\hat{B}_1 = \hat{B}_2$	<p>[\angles opp equal sides \angle^e teenoor gelyke sye]</p> <p>[exterior angle of a cyclic quad/ <i>buite \angle van kvh</i>]</p> <p>[\angles in the same segment \angle^e in dies. \odot segm.]</p>	<p>✓ S/R</p> <p>✓ S ✓ R</p> <p>✓ S R</p> <p>(5)</p>
<p>10.2.2</p>	$\hat{C}_1 + \hat{C}_2 = \hat{D}$ but $\hat{D} = \hat{B}_2$ $\therefore \hat{B}_2 = \hat{C}_1 + \hat{C}_2$ \therefore BECH is a cyclic quad is 'n koordevierh	<p>[tan chord theorem /\angletussen raaklyn en koord]</p> <p>[proved]</p> <p>[exterior \angle = int opp\angle OR converse of ext \angle of cyclic quad / <i>buite \angle van vierhoek = teenoorst. binne \angle</i>]</p>	<p>✓ S/R</p> <p>✓ S ✓ S ✓ R</p> <p>(4)</p>
<p>10.2.3</p>	$\hat{B}_2 = \hat{A}_3 + \hat{T}_1$ but $\hat{B}_2 = \hat{C}_1 + \hat{C}_2$ and $AT = CT$ $\therefore \hat{C}_1 + \hat{C}_2 = \hat{A}_2 + \hat{A}_3$ $\hat{A}_2 + \hat{A}_3 = \hat{A}_3 + \hat{T}_1$ $\therefore \hat{A}_2 = \hat{T}_1$ \therefore CA is a tangent to circle ABT	<p>[exterior \angle of a triangle/ <i>buite \angle van Δ</i>]</p> <p>[proved/ bewys]</p> <p>[tangents from the same point / <i>raaklyne vanuit dies. punt</i>]</p> <p>[\angles opp equal sides / \angle^e teenoor gelyke sye]</p> <p>[\angle between line & chord OR converse of tan chord theorem / \angle tussen lyn en koord = \angle in teenoorst. \odot segm.]</p>	<p>✓ S/R</p> <p>✓ S/R</p> <p>✓ S</p> <p>✓ S</p> <p>✓ R</p> <p>(5) [19]</p>

QUESTION/VRAAG 11



<p>11.1</p>	<p>In ΔPAT and ΔPCA</p> <p>$\hat{P} = \hat{P}$</p> <p>$\hat{A}_1 = \hat{C}_1$</p> <p>$\hat{T}_1 + \hat{T}_2 = \hat{A}_1 + \hat{A}_2$</p> <p>$\therefore \Delta PAT \parallel \Delta PCA$</p>	<p>[common / <i>gemeenskaplik</i>]</p> <p>[tan chord theorem / <i>∠ tussen raaklyn en koord</i>]</p> <p>[∠ sum in Δ OR sum of ∠s in Δ OR Int ∠s Δ / <i>∠^e van Δ</i>]</p> <p>[$\angle\angle\angle$ OR/ OF equiangular / <i>gelykhoekig</i> / $\angle\angle\angle$]</p> <p>✓ S/R</p> <p>✓ S/R</p> <p>✓ R</p> <p>(3)</p>
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11.2.1	$\frac{PA}{PC} = \frac{AT}{CA} = \frac{PT}{PA}$ $PA^2 = PT \cdot PC$ $6^2 = x(x+5)$ $36 = x^2 + 5x$ $x^2 + 5x - 36 = 0$ $(x+9)(x-4) = 0$ $\therefore x = -9 \text{ or / of } x = 4$ $\therefore PT = 4$	$\Delta PAT \parallel \Delta PCA$ ✓ S/R ✓ S ✓ substitution / <i>vervanging</i> ✓ factors / <i>faktore</i> (4)
11.2.2	In ΔAPC $\frac{PD}{PA} = \frac{PT}{PC}$ $\frac{PD}{6} = \frac{4}{9}$ $PD = \frac{(6)(4)}{9}$ $= \frac{8}{3} / 2,67$	[line \parallel one side of Δ OR/OF prop theorem; $DT \parallel AC$ / <i>lyn \parallel een sy van Δ</i>] ✓ S ✓ R ✓ $\frac{PD}{6} = \frac{4}{9}$ ✓ answer / <i>antwoord</i> (4) [11]

TOTAL/TOTAAL [150]